2D characterization of near-surface $V_p/V_s$: surface-wave dispersion inversion versus refraction tomography

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ABSTRACT
The joint study of pressure (P-) and shear (S-) wave velocities ($V_p$ and $V_s$), as well as their ratio ($V_p/V_s$), has been used for many years at large scales but remains marginal in near-surface applications. For these applications, $V_p$ and $V_s$ are generally retrieved with seismic refraction tomography combining P and SH (shear-horizontal) waves, thus requiring two separate acquisitions. Surface-wave prospecting methods are proposed here as an alternative to SH-wave tomography in order to retrieve pseudo-2D $V_s$ sections from typical P-wave shot gathers and assess the applicability of combined P-wave refraction tomography and surface-wave dispersion analysis to estimate $V_p/V_s$ ratio. We carried out a simultaneous P- and surface-wave survey on a well-characterized granite-micaschists contact at Plœmeur hydrological observatory (France), supplemented with an SH-wave acquisition along the same line in order to compare results obtained from SH-wave refraction tomography and surface-wave profiling. Travel-time tomography was performed with P- and SH-wave first arrivals observed along the line to retrieve $V_p$ and $V_s$ models. Windowing and stacking techniques were then used to extract evenly spaced dispersion data from P-wave shot gathers along the line. Successive 1D Monte Carlo inversions of these dispersion data were performed using fixed $V_p$ values extracted from the $V_p$ model and no lateral constraints between two adjacent 1D inversions. The resulting 1D $V_s$ models were then assembled to create a pseudo-2D $V_s$ section, which appears to be correctly matching the general features observed on the $V_s$ model. If the $V_s$ pseudo-section is characterized by strong velocity uncertainties in the deepest layers, it provides a more detailed description of the lateral variations in the shallow layers. Theoretical dispersion curves were also computed along the line with both $V_p$ and $V_s$ models. While the dispersion curves computed from $V_p$ models provide results consistent with the coherent maxima observed on dispersion images, dispersion curves computed from $V_s$ models are generally not fitting the observed propagation modes at low frequency. Surface-wave analysis could therefore improve $V_s$ models both in terms of reliability and ability to describe lateral variations. Finally, we were able to compute $V_p/V_s$ sections from both $V_p$ and $V_s$ models. The two sections present similar features, but the section obtained from $V_s$ shows a higher lateral resolution and is consistent with the features observed on electrical resistivity tomography, thus validating our approach for retrieving $V_p/V_s$ ratio from combined P-wave tomography and surface-wave profiling.

INTRODUCTION
The joint study of pressure (P-) and shear (S-) wave velocities ($V_p$ and $V_s$, respectively), as well as their ratio ($V_p/V_s$), has been used for many years at large scales. $V_p/V_s$ is commonly employed in seismology and geodynamics to study oceanic and continental crusts’ structures (Nicholson and Simpson 1985; Julià and Mejía 2004; Tryggvason and Linde 2006; Powell et al. 2014), subduction and extension zones (Nakajima et al. 2001; Bauer et al. 2003; Latorre et al. 2004; Gautier et al. 2006; Reyners et al. 2006), active volcanic areas (Walck 1988; Sanders et al. 1995; Lees and Wu 2000; Schutt and Humphreys 2004), or earthquake-source regions (Catchings 1999; Ryberg et al. 2012). $V_p/V_s$ has proved to be an efficient parameter to highlight the existence of melt or aqueous fluid
phase (Takei 2002) since the liquid phase affects $V_p$ and $V_s$ differently (Biot 1956a,b).

Many experimental studies (Berryman 1999; Lee 2002; Dvorkin 2008) and theoretical developments (Wyllie et al. 1956; Murphy 1982; Prasad 2002; Uyanik 2011) have been aimed at understanding the effect of saturation and pore fluids on body wave velocities in consolidated media, especially in the field of hydrocarbon exploration where the $V_p/V_s$ ratio is frequently used to discriminate different pore fluids in reservoirs (Tatham and Stoffa 1976; Fu et al. 2006; Rojas 2008). The value of the $V_p/V_s$ ratio is also related to in situ stress orientation (Thompson and Evans 2000), fractures and cracks presence, and pore geometry for individual lithologies with small variations in composition (Tatham 1982; Wilkens et al. 1984).

In near-surface applications (at depth lower than 100 m), the combined study of $V_p$ and $V_s$ is often proposed without the calculation of $V_p/V_s$ ratios. It is classically carried out for engineering purposes to determine the main mechanical properties of reworked materials in active landslides (Godio et al. 2006; Jongmans et al. 2009; Socco et al. 2010b; Hibert et al. 2012), control fill compaction in civil engineering (Heitor et al. 2012; Cardarelli et al. 2014), study weathering and alteration of bedrock (Olna et al. 2010), or assess earthquake site response (Jongmans 1992; Lai and Rix 1998; Raptakis et al. 2000; Othman 2005). More recently, this approach has also been proposed for hydrological applications to characterize shallow aquifers (Grelle and Guadagno 2009; Fabien-Ouellet and Fortier 2014; Pasquet et al. 2015).

For these shallow-target studies, $V_p$ and $V_s$ are generally retrieved with seismic refraction tomography using both P and SH (shear-horizontal) waves (Turesson 2007; Grelle and Guadagno 2009; Fabien-Ouellet and Fortier 2014; Pasquet et al. 2015). The use of this method is widespread since it is easily carried out with a one-dimensional (1D) to three-dimensional (3D) coverage, quick to implement and relatively inexpensive (Galibert et al. 2014). However, if measurements of $V_p$ are performed quite efficiently for many years, retrieving $V_s$ remains complex since it requires the use of horizontal component geophones difficult to set up horizontally (Sambuelli et al. 2014) and specific sources strenuous to use (Sheriff and Geldart 1995; Jongmans and Demanet 1993; Xia et al. 2002; Haines 2007).

An alternative to SH-wave refraction tomography, surface-wave prospecting methods are commonly proposed to achieve indirect estimation of $V_s$ in a relatively straightforward manner (e.g., Gabriels et al. 1987; Jongmans and Demanet 1993; Park et al. 1999; Socco et al. 2004; Socco et al. 2010a). Due to their dispersive nature, surface waves are characterized by an investigation depth that mainly depends on the considered data frequency. Surface waves are thus widely used at large scales in global seismology for mantle investigations using low frequencies. When targeting shallow structures with strong lateral variability, surface-wave methods are, however, limited by the well-known trade-off between lateral resolution and investigation depth (Gabriels et al. 1987). On the one hand, the inverse problem formulation requires the investigated medium to be assumed 1D below the spread, which has to be short enough to achieve lateral resolution and perform two-dimensional (2D) profiling. On the other hand, long spreads and low-frequency geophones are required to record long wavelengths in order to increase the investigation depth and mitigate near-field effects (Russel 1987; Forbriger 2003a,b; O’Neill 2003; O’Neill and Matsuoka 2005; Bodet et al. 2005; Zywicki and Rix 2005; Bodet et al. 2009).

When the seismic set-up provides redundant data, several countermeasures exist to overcome these drawbacks and narrow down the lateral extent of dispersion measurements, such as common mid-point cross-correlation (Hayashi and Suzuki 2004; Grandjean and Bitri 2006; Ikeda et al. 2013), multi-offset phase analysis (Strobbia and Foti 2006; Vignoli and Cassiani 2010), or offset moving windows and dispersion stacking techniques (O’Neill et al. 2003; Bohlen et al. 2004; Nedicuca 2007; Boiero and Socco 2010, 2011; Bergamo et al. 2012).

The joint analysis of travel-time tomography $V_p$ and surface-wave profiling $V_s$ has recently been proposed to retrieve 1D time-lapse $V_p/V_s$ sounding (Pasquet et al. 2015) or 2D $V_p/V_s$ sections (Ivanov et al. 2006; Konstantaki et al. 2013). Pasquet et al. (2015) highlighted an overall consistency between the temporal variations of the water table and $V_p/V_s$ contrasts. For their part, Konstantaki et al. (2013) assessed the lateral fluctuations of a shallow aquifer water table level with 2D $V_p/V_s$ variations. Using a single standard acquisition set-up to retrieve 2D $V_p$ and $V_s$ sections thus appears interesting and convenient to reduce equipment costs and acquisition time. Yet, refraction tomography and surface-wave profiling involve distinct characteristics of the wavefield and different assumptions about the medium, thus providing results of different resolutions and investigation depths difficult to compare to each other.

This study tackles such issues through a systematic comparison of $V_p$ models obtained from SH-wave refraction and surface-wave dispersion inversion, along with $V_p$ retrieved from P-wave refraction, as recently proposed by Pasquet et al. (2014, 2015). For this purpose, we targeted the Pleumeur hydrological observatory (France). This experimental site has been subject to many geophysical and hydrogeological studies aimed at characterizing the flow processes involved in the recharge of the outstandingly productive fractured aquifer present in the region (Touchard 1999; Le Borgne et al. 2006a,b, 2007; Ruelleu et al. 2010; Jiménez-Martínez et al. 2013). The study area is located at a contact between granites and micaschists, clearly highlighted in the surface by electrical resistivity tomography (ERT) and electrical conductivity (EC) mapping. However, previous refraction seismic studies showed that $V_p$ alone was neither able to detect the contact zone nor able to discriminate granites from micaschists, probably because P-wave velocity is mainly controlled by the water content in the weathered areas. The site consequently provided a challenging framework to test the applicability of the joint interpretation of $V_p$ and $V_s$ for near-surface applications. In the present study, $V_p$ and $V_s$ sections were classically obtained with P- and SH-wave travel-time tomography.
carried out on a line intersecting the contact zone. Surface-wave profiling was performed by means of offset moving window and dispersion stacking techniques. Local dispersion measurements were first extracted from different shots illuminating the same portion of the seismic line and then stacked to increase signal-to-noise ratio. The extraction window was eventually moved along the line to retrieve a collection of local multimodal dispersion measurements. Several window lengths were tested to find the best compromise between lateral resolution and investigation depth (Pasquet et al. 2012). The lateral consistency of dispersion data was thoroughly controlled during picking through visual browsing and a posteriori verified on phase velocity pseudo-sections. Separate Monte Carlo inversions of dispersion curves were then performed along the line with no lateral constraints in order to reconstruct a pseudo-2D section. The parameterization of those inversions was based on: (i) $V_p$ obtained from travel-time tomography; (ii) a priori geological knowledge; and (iii) maximum wavelengths observed along the line. Theoretical dispersion curves were then recomputed from both $V_p$ models along the line to control the inversion quality and the consistency of these models. Finally, $V_p/V_s$ obtained from both methods were compared to evaluate their ability to image $V_p/V_s$ variations and assess their practical limitations.

SITE DESCRIPTION AND DATA ACQUISITION

Geological setting

The Plœmeur site is located on the south coast of Brittany (west of France), 3 km far from the Atlantic Ocean, near the city of Lorient (Fig. 1). The crystalline bedrock aquifer present in the area is composed of tectonic units developed during the Hercynian orogeny and marked by numerous synkinematic intrusions of upper Carboniferous leucogranites (Ruelleu et al. 2010). The pumping site is located at the intersection of: (i) a contact between the Plœmeur granite and overlying “Pouldu” micaschists dipping 30° to the North and (ii) a subvertical fault zone striking N 20° (Fig. 1). Weathering in the area is limited to the first few meters, except in the micaschists near the pumping site where it reaches about 30 m. Before the start of the pumping activities in 1991, the site was a natural aquifer discharge area with preferential upward fluxes. The average water levels began to decline during the first years of operation but have stabilized since 1997 (Jiménez-Martínez et al. 2013). Despite the low permeability and porosity of these lithologies, pumping wells implanted in the site have been continuously producing water at a rate of about 10^6 m^3 per year since 1991 (Touchard 1999), with limited head decrease and no seawater intrusion. One of the challenges on this site is to understand recharge processes in these highly heterogeneous systems. For this purpose, the site is monitored by several wells implanted mostly around the contact zone and in the clayey area overlaying micaschists (F* and MF* in Fig. 2).

Previous geophysical results

Slingram EC mapping and ERT were carried out on the site prior to the seismic campaign in order to accurately describe near-surface lithologies. Apparent EC ($\sigma_a$) variations over the first 5.5 m in depth were mapped using an electromagnetic device with low induction number (intercoil spacing of 3.66 m and frequency of 9.8 kHz) in vertical dipole (VD) configuration, integrating conductivity values down to about 6 m in depth (McNeill 1980). We used a continuous acquisition mode following profiles separated with 5 m to 7 m, covering an area of about 15 ha (Fig. 2a). As for ERT, we used a multi-channel resistivimeter with a 96-electrode Wenner-Schlumberger array and 1 roll-along (Fig. 2b). The electrodes were spaced with 4 m in order to obtain a 476-m-long profile roughly oriented west-east (WE on Fig. 2a). The inversion was performed using the RES2DINV software (Loke and Barker 1996).

Results of EC mapping show smooth lateral variations of $\sigma_a$ (from less than 5 mS/m to over 30 mS/m, i.e., from 200 $\Omega$m to less than 30 $\Omega$m in terms of apparent electrical resistivity $\rho_a$) in the subsurface. Western low $\sigma_a$ values are clearly associated with the presence of very shallow granite (between 0 m and 125 m along the WE profile in Fig. 2a). On the contrary, higher $\sigma_a$ values observed in the eastern part can be related to clays overlaying weathered micaschists (between 275 m and 476 m in Fig. 2a).

Such distribution seems in agreement with the assumption of the contact zone striking N 20° in the area. ERT results are also consistent with the anticipated geological structures in depth and clearly match the apparent EC variations in surface (Fig. 2b). Four main structures can be delineated in Fig. 2b: fresh granite (FG), almost outcropping in the western part, characterized by high electrical resistivity ($\rho$) values (around 1000 $\Omega$m); weathered granite (WG), at the surface in the western part, characterized by significantly lower $\rho$ values (around 200 $\Omega$m); clays (CL), at the surface in the eastern part, characterized by slightly lower $\rho$ values (between 50 $\Omega$m and 200 $\Omega$m); and micaschists

FIGURE 1
Geological context of the Plœmeur hydrological observatory and location of the experimentation (modified from Ruelleu et al. (2010) and Jiménez-Martínez et al. (2013)).
same line. We used 72 geophones, a 4-m receiver spacing and 2 roll-alongs to finally obtain a 476-m-long profile (Fig. 3). A 72-channel seismic recorder was used with 14-Hz vertical component geophones for the P-wave and surface-wave profiles and with 14-Hz horizontal component geophones for the SH-wave profile. The use of 14-Hz geophones offers a good compromise to obtain seismic records with a frequency content suitable for surface-wave, refraction, and reflection processing. First shot location was one-half receiver spacing away from the first trace, and move-up between shots was one receiver interval in order to achieve the high coverage required to perform refraction tomography and to stack dispersion data. 219 shots were recorded along each profile for a total number of 15768 active traces. The P-wave source consisted of an aluminium plate hit vertically by a 5-kg sledgehammer. The plate was hit six times at each position to increase signal-to-noise ratio. SH waves were generated with a handheld source consisting of a heavy metal frame hit laterally by a 5-kg sledgehammer. The SH-wave source was hit 12 times at each position.

(MS), deeper in the eastern part, characterized by higher $\rho$ values (around 750 $\Omega$m). Possible evidence of the contact zone is visible between 225 m and 250 m along the ERT profile, marking a strong contrast between WG and clays (hashed area in Fig. 2b). The positions of the nearest piezometric wells are projected on the WE line with their measured piezometric head level. A significant decrease in this level is observed in the wells located in the hashed area due to pumping occurring in the F28 well. While Pasquet et al. (2015) studied in simplified 1D conditions, this site offers the perfect framework to address 2D issues (i.e., presence of strong lateral variations of lithology and topography), especially when knowing that previous P-wave tomography studies failed to depict these lateral variations.

**Seismic acquisition**

The seismic acquisition set-up was deployed along the ERT profile (WE in Fig. 2a). It consisted of a simultaneous P- and surface-wave acquisition followed by an SH-wave acquisition along the same line. We used 72 geophones, a 4-m receiver spacing and 2 roll-alongs to finally obtain a 476-m-long profile (Fig. 3). A 72-channel seismic recorder was used with 14-Hz vertical component geophones for the P-wave and surface-wave profiles and with 14-Hz horizontal component geophones for the SH-wave profile. The use of 14-Hz geophones offers a good compromise to obtain seismic records with a frequency content suitable for surface-wave, refraction, and reflection processing. First shot location was one-half receiver spacing away from the first trace, and move-up between shots was one receiver interval in order to achieve the high coverage required to perform refraction tomography and to stack dispersion data. 219 shots were recorded along each profile for a total number of 15768 active traces. The P-wave source consisted of an aluminium plate hit vertically by a 5-kg sledgehammer. The plate was hit six times at each position to increase signal-to-noise ratio. SH waves were generated with a handheld source consisting of a heavy metal frame hit laterally by a 5-kg sledgehammer. The SH-wave source was hit 12 times at each position.
For both P- and SH-wave acquisitions, the sampling rate was 0.25 ms and the recording time was 2 seconds to include full surface-wave wavefield. A delay of -0.02 seconds was kept before the beginning of each record to prevent early triggering issues. The collected data presented on Fig. 4 are affected with a significant noise level, especially at far offset (80 m and more), due to active pumping wells and military airplanes regularly landing and taking off from a nearby air force base. Seismograms clearly show lateral variations due to both topographic effects and subsurface velocity changes, with strong attenuation over clays and micaschists in the eastern part of the line.

**TRAVEL-TIME TOMOGRAPHY**

**Travel-time data**

We applied DC removal and a zero-phase low-pass filter on both P- and SH-wave data to remove high-frequency noise (>100 Hz) and help for first arrival identification at far offsets. For the P-wave profile, a total of 7076 first arrivals (45% of all traces) were determined (Fig. 5a) and 10352 traces (65% of all traces) were picked on SH-wave shots (Fig. 5c). Travel-time data could not be obtained where noise level was too high (grey dots in Fig. 5), with average maximum offsets around 100 m for P waves and around 150 m for SH waves. Travel times are represented in a source-receiver diagram (Fig. 5), which shows the distribution of first arrival times for each source-receiver pair (Bauer et al. 2010; Baumann-Wilke et al. 2012). The diagonal traces indicate the zero-offset travel times, where source and receiver locations are identical. This representation gives a first impression of the subsurface velocity structure and allows for checking the lateral consistency of picked travel times. Three main areas are clearly visible on both P- and SH-wave first arrivals: the first area (from 0 m to 125 m) is characterized by the shortest first arrival times (i.e., shallow high velocity zone); the area between 125 m and 275 m depicts slightly increasing times; and the third area (from 275 m up to the end of the line) shows greater arrival times (compared with the first area), probably associated with shallow low velocities.

The distribution depicted in Fig. 5a and 5c appears interestingly related to the lateral variability observed on the EC map (Fig. 2a). Along the seismic profile, very low $\sigma_a$ values occur between 0 m and 125 m on the granite side and are coherent with short first arrival times. High $\sigma_a$ values observed between 275 m and the end of the line are also consistent with the shallow low velocity zone suggested by long first arrival times. In the center part (from 125 m to 275 m), intermediate apparent EC values are in agreement with slightly decreasing shallow velocities observed in Fig. 5a and 5c, suggesting a thickening of the weathered layer.

**Tomography inversion**

Travel-time data were inverted with the refraction tomography software RAYFRACT (Schuster and Quintus-Bosz 1993; Sheehan et al. 2005; Rohdewald 2011) using a smooth gradient initial model. This model is the 2D extension of the mean 1D model obtained directly from picked travel times, assuming velocity gradients in a 1D tabular medium (Gibson et al. 1979). It varied from 10 m/s at the surface to 3500 m/s at 40 m in depth for the P-wave model and from 10 m/s at the surface to 2000 m/s at 40 m in depth for the SH-wave model. The inversion process was stopped when velocity update, global root-mean-square (RMS) error, and maximum normalized residual reached minimum values. In addition, 30 iterations were needed for both P- and SH-wave travel times. For the P-wave profile, the global RMS error (in blue in Fig. 6b) and the maximum normalized residual (in red in Fig. 6b) both steeply decrease during the first six iterations, i.e., from 5 ms to 2.5 ms and from 25 ms to 13 ms, respectively, and more gradually during the last iteration steps until they both reach minimum values of 2.1 ms and 11.5 ms, respectively. Mean velocity update also rapidly decreases to reach a minimum value after six iterations (in black in Fig. 6c). Maximum and minimum velocity updates (in red and blue, respectively, in Fig. 6c) are more perturbed and tend to stabilize only after 20 iterations. As for SH-wave data, the global RMS error (in blue in Fig. 6e) and the maximum...
the last iteration steps until they both reach minimum values of 4.3 ms and 20.1 ms, respectively. Mean, maximum, and minimum velocity updates (in black, red, and blue, respectively, in normalized residual (in red in Fig. 6e) both quickly decrease during the first 10 iterations, i.e., from 12.5 ms to 6 ms and from 50 ms to 22 ms, respectively, and more smoothly during the first 10 iterations, i.e., from 12.5 ms to 6 ms and from 50 ms to 22 ms, respectively, and more smoothly during

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Normalized residuals were computed between observed and calculated travel times for every picked trace (Bauer et al. 2010). Their distributions are represented in source-receiver diagrams for both P- (Fig. 5b) and SH-wave (Fig. 5d) travel times. P-wave inversion results have lower global RMS values (2.1 ms for P waves; 4.3 ms for SH waves) and maximum residual values (11.5 ms for P waves; 20.1 ms for SH waves), and the mean residual value is higher for P waves (6.7%) than for SH waves (3.9%). The ratio of residuals below 10% is also higher for SH-wave models (around 93%) than for P-wave models (around 91%). The distribution of residuals shows the highest values at near offsets, probably due to shallow lateral heterogeneities and triggering issues during the acquisition.

The final velocity models were clipped for both $V_p$ (Fig. 6a) and $V_s$ (Fig. 6d) sections below a ray coverage of 100 rays per grid cell to keep only well-resolved areas. Both models are characterized by velocities mainly following a linearly increasing trend in depth and show no strong lateral variations. Only slight perturbations of the initial gradient model along the line can be observed with: (i) higher $V_p$ and $V_s$ in the western part ($HV_p$ and $HV_s$, respectively), corresponding to the high electrical resistivity values associated with FG; (ii) lower $V_p$ in the center ($LV_p$), consistent with a decrease in the piezometric head level and evidences of the contact zone inferred from ERT; and (iii) lower $V_s$ in the eastern part of the profile ($LV_s$).

### SURFACE-WAVE PROFILING

**Extraction of dispersion curves**

Our multifold acquisition set-up allowed us to obtain surface-wave dispersion images from P-wave shot gathers using windowing and dispersion stacking to narrow down the lateral extent of dispersion measurements and increase the signal-to-noise ratio. Dispersion stacking was performed following the basic workflow derived from O’Neill et al. (2003).

1. Select $nW$ traces centered on a specific position along the line $(X_{mid})$.
2. Load a shot illuminating the selected spread.
3. Window the $nW$ traces in the selected shot record.
4. Transform the wavefield to the frequency-phase velocity domain (dispersion image).
5. Normalize amplitude spectrum at each frequency.
6. Repeat steps 2–5 for the $nS$ selected shots.
7. Stack all normalized dispersion images and pick the dispersion curves for each identified propagation mode from the final image.
8. Shift the window of $dW$ traces to the next $X_{mid}$ and repeat steps 1–7.

As aforementioned, the difficulty is to find the best compromise between investigation depth, spectral resolution, and lateral resolution while keeping the 1D assumption valid. Thus, we first performed trial-and-error tests (Pasquet et al. 2012) to select the

![Figure 6](image_url)
optimum window size ($nW$) and the number of sources ($nS$), keeping in mind that there is not, for the moment, any perfect criterion (Pérez Solano 2013; Pérez Solano et al. 2014). A 20-m-wide window with six traces ($nW = 6$) was eventually used with six direct and six reverse shots on each side of the window ($nS = 6$). Using more sources is likely to increase signal-to-noise ratio and enhance the maxima but would narrow down the effective study area along the line (black dots in Fig. 2a).

Single dispersion images were obtained from each shot using a slant stack in the frequency domain (Russel 1987; Mokhtar et al. 1988). These images (in which maxima should correspond to Rayleigh-wave propagation modes) were first compared to confirm the validity of the 1D approximation below the spread (Jongmans et al. 2009). These 12 single dispersion images were then stacked as a final dispersion image. The moving window was finally shifted along the line with a step of one receiver spacing ($dW = 1$, i.e., 4m). We thus obtained evenly spaced dispersion images at each spread mid-point ($X_{mid}$) with a large overlap in order to retrieve smoothly varying dispersion images between two adjacent stacking windows and help for visual browsing when picking dispersion curves.

We eventually obtained a collection of 105 stacked dispersion images along the line, on which coherent maxima associated with the different propagation modes were identified. Visualization of adjacent stacked dispersion images allowed for following the progressive lateral evolution of the different modes and for avoiding mode misinterpretation (Zhang and Chan 2003; O’Neill and Matsuoka 2005; Boaga et al. 2013; Ezersky et al. 2013). These maxima were finally extracted on each stacked dispersion image with an estimated standard error in phase velocity defined according to the workflow described in O’Neill (2003). The dispersion lateral variability is illustrated here by two examples at both sides of the line (Fig. 7a, $X_{mid} = 50$ m and 7c, $X_{mid} = 402$ m).

As, for instance, recommended by Bodet (2005) and Bodet et al. (2009), dispersion curves were limited down to frequencies ($f_{lim}$) where the spectral amplitude of the seismogram became too low (13.5 Hz in Fig. 7b and 8 Hz in Fig. 7d). Several authors (e.g., O’Neill 2003; Zywicki and Rix 2005) also mentioned that wavelengths higher than 50% of the spread length should not be used in order to mitigate near-field effects and prevent from velocity underestimation at low frequency.

These recommendations are only basic rules of thumb mostly valid when using the fundamental mode only. Here, we used wavelengths higher than 50% of our spread length since we were able to perform dispersion stacking and use higher modes, which are of great constraint on the inversion with a strong impact on the investigation depth (Gabriels et al. 1987; Xia et al. 2003). Furthermore, possible low-frequency discrepancies were limited by attributing important errors to dispersion data with respect to frequency and spread length (O’Neill 2003). Finally, the corresponding maximum wavelength ($\lambda_{max}$) was extracted (35 m in Fig. 7a and 37 m in Fig. 7c) to retrieve $\lambda_{max}/2$, a typical investigation depth criterion (O’Neill 2003).

Up to four propagation modes were observed along the line and identified as fundamental (0), first (1), second (2), and third (3) higher modes (only modes up to 2 were identified in the examples shown in Fig. 7). The resulting dispersion curves are presented in Rayleigh-wave phase velocity pseudo-sections as a function of the wavelength $\lambda$ and the spread mid-point $X_{mid}$.

**FIGURE 7**
Dispersion images extracted on both sides of the seismic profile (a, $X_{mid} = 50$ m, and c, $X_{mid} = 402$ m) from six direct and six reverse shots with a six-trace (20-m-wide) window. $X_{mid}$ is the position of the spread mid-point along the line. Spectral amplitude of the far offset direct shot is represented for both examples (b, $X_{mid} = 50$ m, and d, $X_{mid} = 402$ m). Picked dispersion curves are represented for the fundamental (0), first (1), and second (2) higher modes, with error bars defined according to the workflow described in O’Neill (2003). Dispersion curves were limited down to the frequency ($f_{lim}$) where the spectral amplitude of the seismogram became too low. The corresponding maximum wavelength ($\lambda_{max}$) was also extracted to indicate typical investigation depth criterion.
and thickness of each layer) using the following misfit function (MF):
\[
MF = \frac{1}{N_f} \sum_{i=1}^{N_f} \left( \frac{V_{cal} - V_{obs}}{\sigma_i} \right)^2
\]

with \(V_{cal}\) and \(V_{obs}\) being the calculated and observed phase velocities at each frequency \(f_i\), \(N_f\) being the number of frequency samples, and \(\sigma_i\) being the phase velocity measurement error at each frequency \(f_i\).

An appropriate choice of these parameters is considered as a fundamental issue for the successful application of inversion (Socco and Strobbia 2004; Renalier et al. 2010). Based on site a priori geological knowledge (presence of weathering gradients), we used parameterization with a stack of ten layers overlaying the half-space to look for a velocity gradient. The thickness of each layer was allowed for ranging from 0.5 m to 2.5 m. The maximum half-space depth (HSD) is of great importance since it depends on the poorly known investigation depth of the method. It was fixed to the half of the maximum wavelength observed along the entire line (25 m), as recommended by O’Neill (2003) and Bodet et al. (2005). The valid parameter range for sampling velocity models was 10 m/s–1500 m/s for \(V_p\) (based on dispersion observations and refraction tomography), with velocities constrained to only increase with depth, based on geological a priori information. P-wave velocity being of weak constraint on surface-wave dispersion, only the S-wave velocity profile can be interpreted (Der and Landisman 1972; Russel 1987). However, an identical layering is required for \(V_p\) and \(V_s\) in order to interpret
ratios. For this purpose, we extracted an average \( m^3 \) since its influence on dispersion curves is very limited (Der from unrealistic values always remained between 0.1 and 0.5 in order to prevent values were allowed to vary in such a way that Poisson’s ratio in each layer of the inversion parameterization. Furthermore, \( \lambda_{max}/2 \) is given (solid black line in Fig. 9b and 9d) to show where inverted models expand below typical investigation depth criterion. Normalized residuals between observed and calculated phase velocities were computed along the line for each individual sample of the picked dispersion curves. Their distributions are represented in pseudo-sections to control the quality of the final pseudo-2D \( V_p \) section. The fundamental mode residuals’ pseudo-section (Fig. 10e) shows quite uniform values, with a maximum of 19%, a mean residual of 5%, and 86% of the residuals with values below 10%. Residual values obtained for the first higher mode (Fig. 10b) present higher values, especially at great wavelength. The maximum residual value is 29%, the mean is 9%, and only 62% of the residuals are below 10%. As for the second and the third higher modes (Fig. 10c and 10d, respectively), residuals remain very low with a maximum of 12% and 3%, respectively, and a mean residual of 1.8% and 1.3%, respectively. In addition, 99% of the second higher mode samples have residual values below 10%, whereas all samples of the third higher mode have residuals below 10%. We additionally computed the misfit for each 1D \( V_p \) model along the line with equation (1) (Fig. 10e). Misfit values remain stable along the line and range from 0.05 to around 0.25, with a mean value of about 0.125. Several gaps are present along the line and correspond to inversions where none of the calculated models were fitting the error bars.

Each 1D \( V_p \) model was then represented at its corresponding \( Xmid \) position to obtain a pseudo-2D \( V_p \) section (Fig. 11). All the models were represented down to the maximum HSD (25 m), with the investigation depth criterion \( \lambda_{max}/2 \) superimposed in hashed red line. With such a representation, the actual HSD of each model can be easily followed along the line and compared with the investigation depth criterion. If the lateral variations of \( V_p \) values remain remarkably smooth in the shallow layers, the deepest layers and the half-space present an important variability of \( V_p \) caused by the higher uncertainties in dispersion measurements at great wavelength (i.e., higher residual values in Fig. 10). Global results show a shallow low velocity layer (~250 m/s), which is thinner in the western part of the line (from 3 m to 6 m) and becomes thicker (~10 m) in the eastern part. High velocities (between 500 m/s and 1000 m/s) can be observed in the western part, directly below the shallow low velocity layer, whereas the velocity of the half-space remains below 500 m/s in the eastern part.

\[ V_p/V_s \text{ ratios. For this purpose, we extracted an average } V_p \text{ value for each 2.5-m-thick slice of the } V_p \text{ model obtained from refraction tomography (Fig. 6a). This average value was then used to fix } V_p \text{ in each layer of the inversion parameterization. Furthermore, } V_p \text{ values were allowed to vary in such a way that Poisson’s ratio values always remained between 0.1 and 0.5 in order to prevent from unrealistic } V_p \text{ values. Density was set as uniform (1800 kg/m}^3 \text{) since its influence on dispersion curves is very limited (Der and Landsman 1972; Russel 1987). It is worth mentioning that, except for the } V_p \text{ values, we used the same parameterization for all the 1D inversions performed along the line. We assumed that stacking and windowing already naturally smoothed the dispersion data, thus not requiring the use of lateral constraints between successive inversions.}

A total of 63000 models were generated with NA (Fig. 9a, \( Xmid = 50 \text{ m and c, } Xmid = 402 \text{ m} \). Models matching the observed data within the error bars were selected, as suggested by Endrun et al. (2008). The accepted models were used to build a final average velocity model associated with the center of the extraction window (dashed line in Fig. 9b, \( Xmid = 50 \text{ m and 9d, } Xmid = 402 \text{ m} \). As the maximum HSD remains constant along the line (same parameterization for each inversion), \( \lambda_{max}/2 \) is given (solid black line in Fig. 9b and 9d) to show where inverted models expand below typical investigation depth criterion. Normalized residuals between observed and calculated phase velocities were computed along the line for each individual sample of the picked dispersion curves. Their distributions are represented in pseudo-sections to control the quality of the final pseudo-2D \( V_p \) section. The fundamental mode residuals’ pseudo-section (Fig. 10e) shows quite uniform values, with a maximum of 19%, a mean residual of 5%, and 86% of the residuals with values below 10%. Residual values obtained for the first higher mode (Fig. 10b) present higher values, especially at great wavelength. The maximum residual value is 29%, the mean is 9%, and only 62% of the residuals are below 10%. As for the second and the third higher modes (Fig. 10c and 10d, respectively), residuals remain very low with a maximum of 12% and 3%, respectively, and a mean residual of 1.8% and 1.3%, respectively. In addition, 99% of the second higher mode samples have residual values below 10%, whereas all samples of the third higher mode have residuals below 10%. We additionally computed the misfit for each 1D \( V_p \) model along the line with equation (1) (Fig. 10e). Misfit values remain stable along the line and range from 0.05 to around 0.25, with a mean value of about 0.125. Several gaps are present along the line and correspond to inversions where none of the calculated models were fitting the error bars.
QUALITATIVE COMPARISON OF VELOCITY MODELS AND RESULTING $V_p/V_s$

The comparison of velocity models obtained from P-wave tomography ($V_p^{\text{P}}$, Fig. 6a), SH-wave tomography ($V_p^{\text{SH}}$, Fig. 6b), and surface-wave dispersion profiling ($V_p^{\text{sw}}$, Fig. 11) provided results that are consistent with the main structures interpreted from ERT data (Fig. 2b). However, velocity models do not provide such a clear delineation of these structures, especially for $V_p^{\text{P}}$ and $V_p^{\text{SH}}$ sections. Indeed, the travel-time tomography method smoothes the lateral variations of velocity and often suffers from the strong influence of triggering issues on short travel times, which mainly affect the reconstruction of shallow structure velocities. As for surface-wave profiling, the overlaying of structures delimited by ERT on the $V_p^{\text{sw}}$ pseudo-2D section (Fig. 11) confirms the lateral consistency of both $V_p$ models in the first 20 m in depth. If the surface-wave method is clearly limited by its low investigation depth in this case, it provides more information regarding the lateral variations of shallow layers’ velocities and seems to detect the modifications of mechanical properties occurring in the contact zone.

At both Xmid = 50 m (Fig. 12a) and Xmid = 402 m (Fig. 12d), 1D models of $V_p$ and $V_s$ extracted from tomography sections ($V_p^{\text{P}}$ in green solid line and $V_p^{\text{SH}}$ in green dashed line, respectively) are characterized by similar trends of continuously increasing velocities in depth. Furthermore, 1D $V_p^{\text{sw}}$ models (red solid line) show the presence of two constant velocity layers followed by a linearly increasing velocity layer overlaying the half-space. Despite a low investigation depth, the $V_p^{\text{sw}}$ pseudo-section man-

FIGURE 10
Pseudo-section of Rayleigh-wave phase velocity normalized residuals for the fundamental (a), first (b), second (c), and third (d) higher modes along the line after dispersion stacking. $\lambda$ is the wavelength. (e) Misfit values calculated with equation (1) for each 1D inversion along the line.

FIGURE 11
Pseudo-2D $V_p$ section constructed with all 1D $V_p$ models obtained from surface-wave profiling, overlaid with limits interpreted from ERT results. $\lambda_{\max}/2$, represented with a red dashed line, corresponds to a typical investigation depth criterion. Positions of the nearest monitoring wells are projected along the WE line as in Fig. 2b.
models provide the best fit with the picked dispersion curves and the coherent maxima observed on dispersion images, supporting the validity of the final model averaged from all models fitting the error bars. For their part, dispersion curves computed from models are generally not well fitting the observed propagation modes at low frequency, leading us to question the validity of the tomographic model in the deepest layers. After cross-validating both models, we computed ratios along the line with: (i) and (ii) (Fig. 13a) and (ii) and (iii) (Fig. 13b). As a control of both models, forward modelling was performed along the line (examples for $X_{mid} = 50$ m and $X_{mid} = 402$ m are shown in Fig. 12c and 12f, respectively). On the one hand, theoretical dispersion curves were computed using 1D $V_p$ models obtained from SH-wave refraction interpretation ($V_p^{\text{tomo}}$, green solid line) and surface-wave dispersion inversion ($V_s^{\text{sw}}$, red solid line) at $X_{mid} = 50$ m (a) and $X_{mid} = 402$ m (d). 1D $V_p$ models obtained from P-wave refraction tomography ($V_p^{\text{tomo}}$, green dashed line) and resampled to follow the layering of $V_p^{\text{tomo}}$ ($V_p^{\text{tomo}}$, red dashed line) are also represented in (a) and (d). 1D $V_p$/$V_s$ models constructed from $V_p^{\text{tomo}}$ and $V_s^{\text{tomo}}$ ($V_p^{\text{tomo}}/V_s^{\text{tomo}}$, red solid line) and from $V_p^{\text{tomo}}$ and $V_s^{\text{tomo}}$ ($V_p^{\text{tomo}}/V_s^{\text{tomo}}$, green solid line) at $X_{mid} = 50$ m (b) and $X_{mid} = 402$ m (e). The water table level is represented with a black dashed line. In (a) and (b), the water table level is extrapolated from the nearest representative well implanted in the granite (around 100 m west from $X_{mid} = 50$ m). In (d) and (e), the water table level is interpolated from levels measured in wells MF2 and F36 (Fig. 2). Stacked dispersion image obtained at $X_{mid} = 50$ m (c) and $X_{mid} = 402$ m (f). The fundamental (0), the first (1), second (2), and third (3) higher modes’ dispersion curves calculated from $V_p$ and $V_s$ (in red) and from $V_p^{\text{tomo}}$ and $V_s^{\text{tomo}}$ (in green) are superimposed on both images.

As a control of both $V_s$ models, forward modelling was performed along the line (examples for $X_{mid} = 50$ m and $X_{mid} = 402$ m are shown in Fig. 12c and 12f, respectively). On the one hand, theoretical dispersion curves were computed using 1D $V_p^{\text{tomo}}$ and $V_s^{\text{tomo}}$ models (green solid line). On the other hand, theoretical dispersion curves were calculated using 1D $V_p$ models and 1D $V_s^{\text{tomo}}$ models resampled in depth according to the $V_s^{\text{tomo}}$ layering ($V_s^{\text{tomo}}$) (red solid line). $V_s^{\text{tomo}}$ models provide the best fit with the picked dispersion curves and the coherent maxima observed on dispersion images, supporting the validity of the final $V_s^{\text{tomo}}$ model averaged from all models fitting the error bars. For their part, dispersion curves computed from $V_p^{\text{tomo}}$ models are generally not well fitting the observed propagation modes at low frequency, leading us to question the validity of the tomographic model in the deepest layers.

After cross-validating both $V_s$ models, we computed $V_p$/$V_s$ ratios along the line with: (i) $V_p^{\text{tomo}}$ and $V_s^{\text{tomo}}$ (Fig. 13a) and (ii) $V_p^{\text{tomo}}$ and $V_s^{\text{tomo}}$...
and $V_p/V_s$ (Fig. 13b). The $V_p/V_s$ section shows smooth lateral variations, with low $V_p/V_s$ (~1.5) in the western (from 0 m to 150 m) and central (from 200 m to 250 m) parts, separated by intermediate values (~2.25). The eastern part is characterized by higher values (around 2.5 and up to 3.5). At first sight, the $V_p/V_s$ section might look different, especially in the beginning of the line (from 0 m to 275 m), where anomalous high $V_p/V_s$ values are observed around 5 m to 10 m depth. At these depths, the $V_p/V_s$ model presents mostly constant velocities, whereas the $V_p$ model is characterized by linearly increasing velocities.

This incompatibility can thus explain the $V_p/V_s$ discrepancies observed in this layer. With this in mind, we were yet able to delineate different $V_p/V_s$ areas, which correspond well to those observed on the $V_p/V_s$ section. These different areas and the observed $V_p/V_s$ values are also consistent with the main structures delineated in the ERT results (Fig. 2b), whereas it was not clear on $V_p$ or $V_s$ only.

Moreover, 1D $V_p/V_s$ ratios extracted at Xmid = 50 m (Fig. 12b) and Xmid = 402 m (Fig. 12e) from $V_p/V_s$ (red solid line) and $V_p/V_s$ (green solid line) show similar trends. Stronger contrasts and higher ratio values are yet observed on surface-wave analysis results. $V_p/V_s$ values observed at Xmid = 50 m are overall low (below 2.75) with both methods. The water table level extrapolated from the nearest representative piezometric well implanted in the granite (around 100 m west from Xmid = 50 m) is not consistent with any of the contrasts observed on the $V_p/V_s$ models. Indeed, the estimated water table level (~20 m) is close to the maximum HSD where $V_p/V_s$ becomes poorly resolved. Furthermore, no strong $V_p/V_s$ variations can be anticipated in such low-permeability and low-porosity materials (Takei 2002). At Xmid = 402 m, shallow high $V_p/V_s$ ratio values (around 4) are consistent with a wet soil, whereas a strong contrast at 11.5 m deep remarkably matches the water table level interpolated from levels measured in MF2 and F36 (black dashed line). This feature is confirmed on the pseudo-2D $V_p/V_s$ section in the eastern part (Fig. 13a).

CONCLUSIONS
In order to assess the applicability of combined P-wave refraction tomography and surface-wave dispersion analysis to estimate $V_p/V_s$ ratio in near-surface applications, we performed seismic measurements on a well-known granite-micaschists contact at Plœmeur hydrological observatory (France). A simultaneous P- and surface-wave survey was achieved using a single acquisition set-up and was supplemented with an SH-wave acquisition along the same line in order to compare results obtained from SH-wave refraction tomography and surface-wave profiling.

P- and SH-wave first arrivals observed along the line were used to perform travel-time tomography and retrieve $V_p$ models. Successive 1D Monte Carlo inversions of these dispersion data were achieved using fixed $V_p$ values extracted from the $V_p$ model and no lateral constraints between two adjacent 1D inversions. The resulting 1D $V_p$ models were then assembled to create a pseudo-2D $V_p$ section. We computed normalized residuals between observed and calculated phase velocities along the line to control the quality of the $V_p$ model. The model is however char-
acterized by strong velocity uncertainties in the deepest layers. The recomputation of theoretical dispersion curves along the line also provided results that are consistent with the measured dispersion images and proved to be a reliable tool for validating $V_p$ models obtained from SH-wave refraction tomography and surface-wave profiling. Finally, we were able to compute $V_p$ sections from both $V_p^{SW}$ and $V_p^{SH}$. The two sections present similar features, but the section obtained from $V_p^{SW}$ shows a higher lateral resolution, which is consistent with the features observed on ERT, thus validating our approach for retrieving $V_p$ ratio from combined P-wave tomography and surface-wave profiling. Furthermore, the $V_p$ ratios obtained in the clay and micaschist area show a strong contrast consistent with the observed water table level.

An incompatibility, however, remains between $V_p^{SW}$ and $V_p^{SH}$, which can lead to anomalous $V_p$ values. Indeed, travel-time tomography provides a smooth 2D reconstruction of the medium along ray paths propagating from sources to sensors in a narrow frequency band. The investigation depth is strongly related to the length of the acquisition profile and the maximum offset between sources and receivers. Furthermore, the medium is described as a function of the ray coverage, which is strongly related to the spacing between sensors and usually increases in high-frequency zones. For their part, surface-wave methods allow for reconstructing pseudo-2D $V_p$ sections by juxtaposing single 1D models obtained along the line. In this case, the spectral resolution and the investigation depth are a function of the frequency and increase with the length of the recording array, whereas the lateral resolution is inversely correlated with the individual array length. In order to retrieve $V_p$ and $V_s$ models more suited for $V_p$ computation, a joint inversion approach combining Rayleigh and P-guided waves dispersion data along with P-wave refraction travel times could be developed, in the continuation of Maraschini et al. (2010), Pratt et al. (2013) and Boiero et al. (2013b) works.

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